

Calculus

Chapter 7: Differential Equations and More Riemann Sums

Lesson 1: Differential Equations - An Introduction

Question #1

Reference Q.667

Solve the following differential equation with the given initial value.

$$\frac{dy}{dx} = x^{\frac{2}{3}}, y(1) = 0$$

Question #2

Reference Q.668

Solve the following differential equation with the given initial value.

$$\frac{dy}{dx} = \cos x + 2x, y(0) = 2$$

Question #3

Reference Q.669

Find the equation that has a slope at any point (x,y) equal to $y' = 3x + 4$, and that passes through the point (0, -3).

Question #4

Reference Q.670

If the 2nd derivative of a function is equal to some constant "k" (i.e. $f''(x) = k$), find $f(x)$ in general (i.e. leave any constants of integration as C_1 or C_2 , etc)

Question #5

Reference Q.671

Show that $y = 5e^x + 3\sin x + 2$ is a solution of the initial-value problem $y' = 5e^x + 3\cos x$, with $y(0) = 7$.

Question #6

Reference Q.672

Solve the following differential equation by separation of variables.

$$\frac{dy}{dx} = \frac{\sec^2 2x - 3x^2}{\cos y - 8e^{3y}} \text{ with } y(0) = 0.$$

Question #7

Reference Q.673

Solve the following differential equation by separation of variables.

$$\frac{dy}{dx} = \frac{y^2}{x}$$

Question #8

Reference Q.674

Solve the following differential equation by separation of variables.

$$\frac{dy}{dx} = \frac{x+2}{3y+3}, y(0) = 0$$

Question #9

Reference Q.675

Solve the following differential equation by separation of variables.

$$y' = 5(\sin x + 1)e^{3y}$$

Question #10

Reference Q.676

Solve the following differential equation by separation of variables.

$$\sin y(x^5 - 3 \ln x) \frac{dy}{dx} = \frac{3}{x} - 5x^4$$

Question #11

Reference Q.677

Solve the following differential equation by separation of variables.

$$\sqrt{x} \frac{dy}{dx} = \frac{3e^{\sqrt{x}}}{(3 \csc^2 y + \sec^2 2y)}$$

Question #12

Reference Q.678

Solve the following differential equation by separation of variables.

$$\frac{\sqrt{x^2 + 5} dy}{dx} = 2x(y + 3)$$

Question #13

Reference Q.679

A Petri dish of a certain bacteria grows at a rate of 3% per hour. If the dish contains 2000 bacteria to start with and $P(t)$ is the population of bacteria after t hours:

- What is the formula for $P(t)$?
- How long until the bacteria doubles to 4000?
- How long will it take to reach a population of 7500?

Question #14

Reference Q.680

A new National Parks Reserve is estimated to be able to hold a maximum of **4,000** deer. Assuming we have exponential growth at 2.5% per year in the reserve, and we begin with **200** deer, how long will it take until the Park is at capacity in terms of the number of deer?

Question #15

Reference Q.681

A type of bacteria Parks Reserve has an initial population of 3000 divides in half every **3 hours** in a certain environment. Suppose $P(t)$ is the population after t hours. If the culture grows according to an exponential model:

- What is the equation for $P(t)$.
- How many cells are there after 1 day?
- How many days would it take for 10 cells to be left?

Question #16

Reference Q.682

If the half-life of a substance is 12.21 hours, how many hours until this substance is reduced to 1% of its initial amount?

Question #21

Reference Q.9267

If $\frac{dy}{dx} = xy^2 + x$, find the general solution for y .

Question #17

Reference Q.683

The following question follows an exponential growth or decay model. Solve for $y(t)$

If $y(0) = 2$ and the growth rate is **3.5 %**

Question #18

Reference Q.684

The following question follows an exponential growth or decay model. Solve for $y(t)$

If $y(0) = 20$ and the rate of decay is **1.7%**

Question #19

Reference Q.685

The following question follows an exponential growth or decay model. Solve for $y(t)$ if $y(2) = 4$ and the half-life is 2 years.

Question #20

Reference Q.686

The following question follows an exponential growth or decay model. Solve for $y(t)$

if $y(2) = 4$ and in 10 yrs it doubles.

Question #22

Reference Q.9269

A population P grows according to the equation $\frac{dP}{dt} = kP$, where k

is some real number and t is time in years. If the population triples every 20 years, then what is the value of k ?